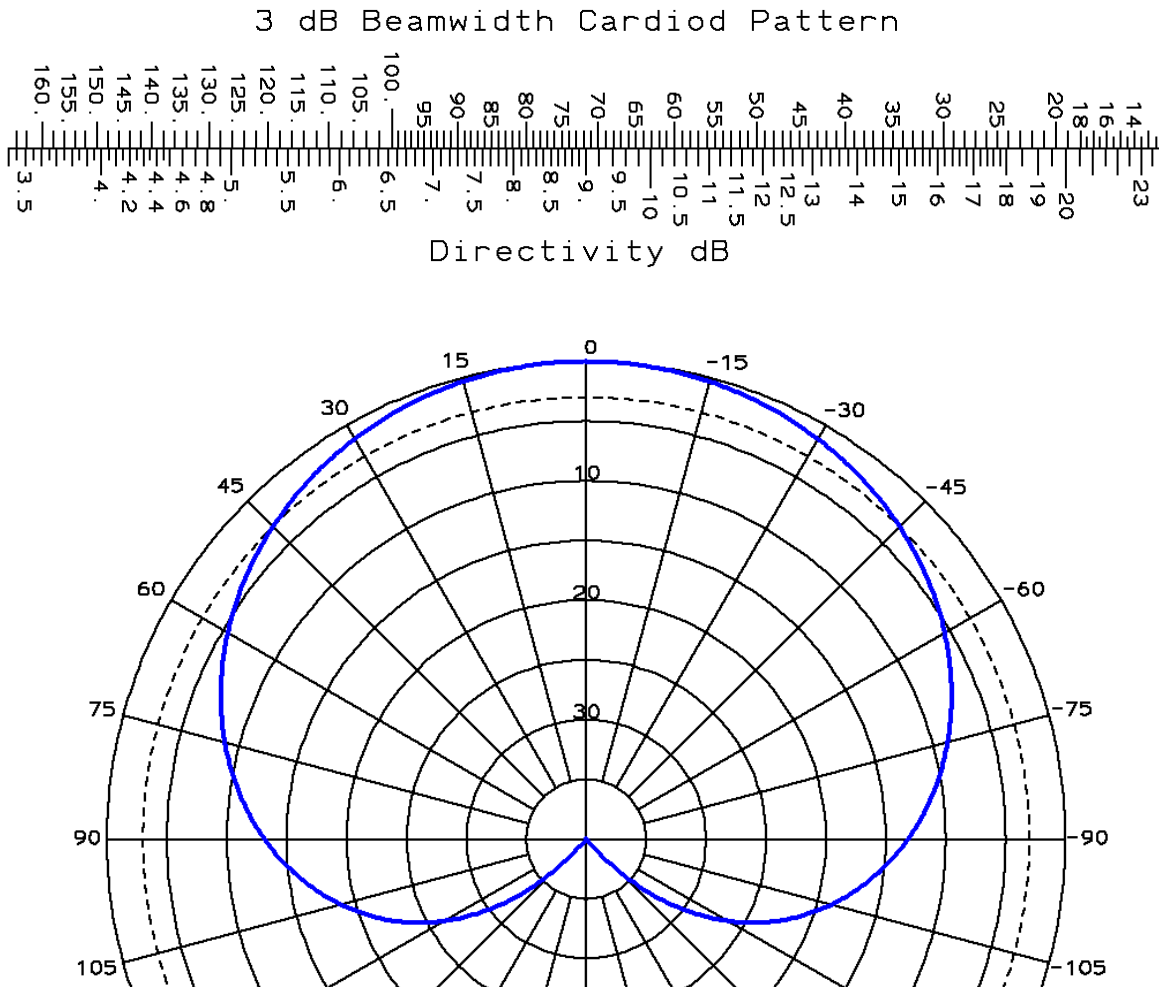
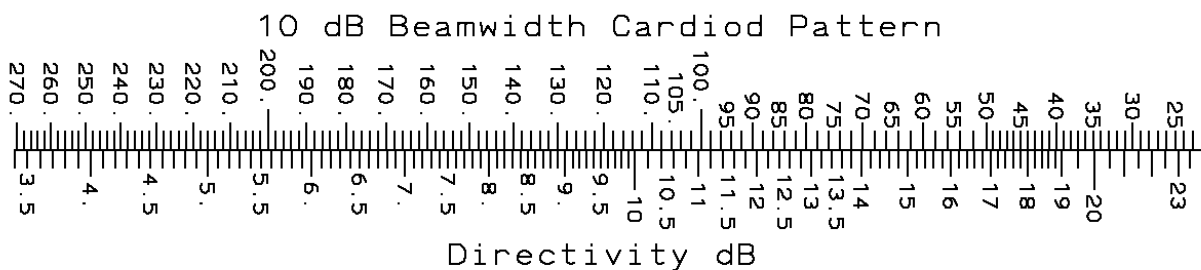


### 1-8.1.1 Pencil Beam Results of Directivity given Beamwidths

Cardioid pattern  $E(\theta) = \cos^N(\theta/2)$  with equal beamwidths in the principal planes as shown in Figure 1-8.1.-1 is converted directivity by the scales below. The program **WIDEDIR** computes directivity in a DOS window given  $E$ - and  $H$ -plane beamwidths by using the elliptical approximation of Eq. (1-21).



**Figure 1-8.1.1-1** Cardioid pattern  $E(\theta) = \cos^N(\theta/2)$



### Gaussian beam pattern directivity given either 3- or 10-dB beamwidth

The Gaussian beam feed (see Section 7-5) has a more complicated expression than the approximation  $E(\theta) = \cos^N(\theta/2)$  and similar looking patterns. However, this feed satisfies the Helmholtz equation and gives correct results when using geometry optics analyses for a parabolic reflector. It also has expressions that produce better near-field results. The program **WIDEDIR** computes directivity in a DOS window given  $E$ - and  $H$ -plane beamwidths by using the elliptical approximation of Eq. (1-21).

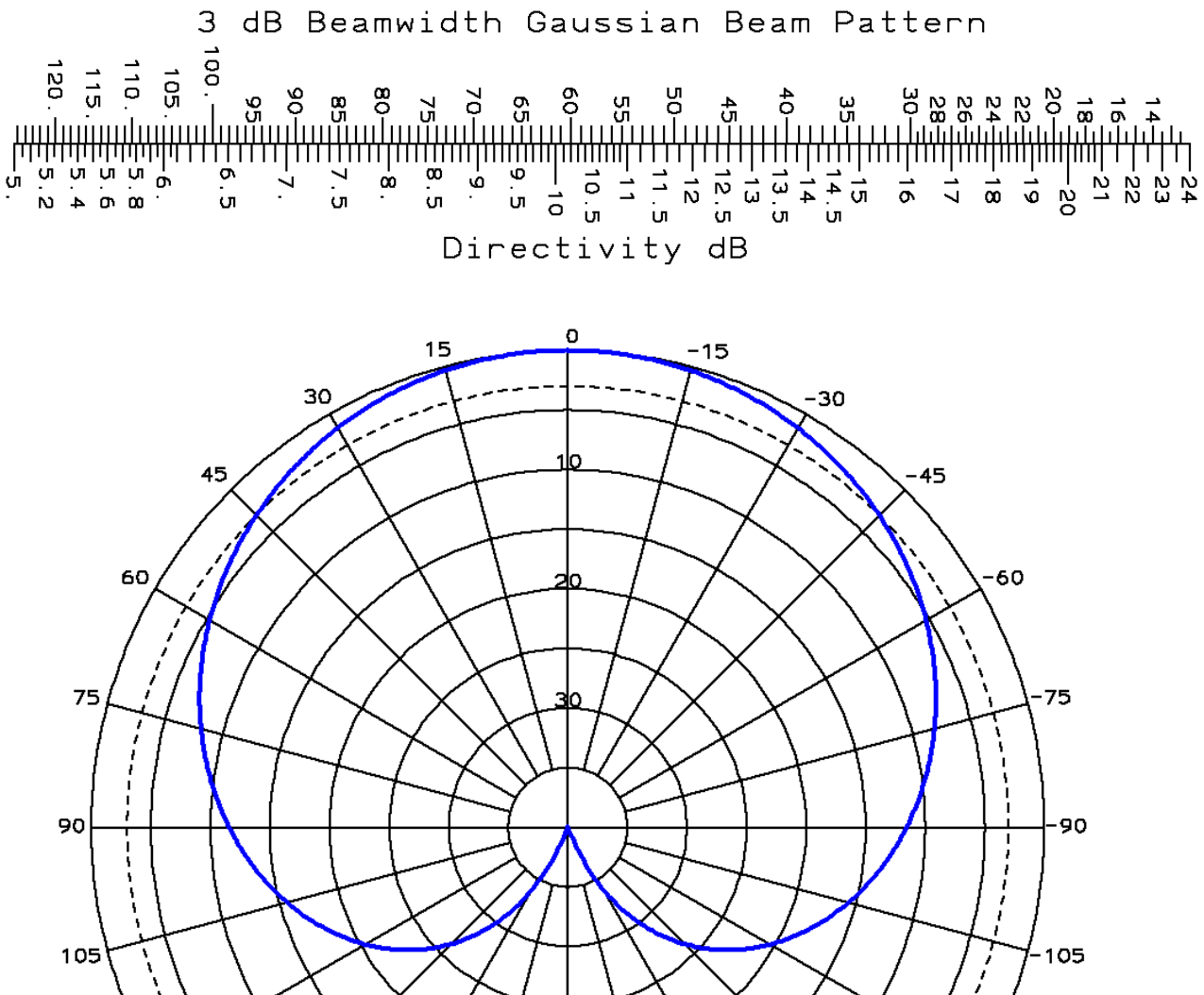


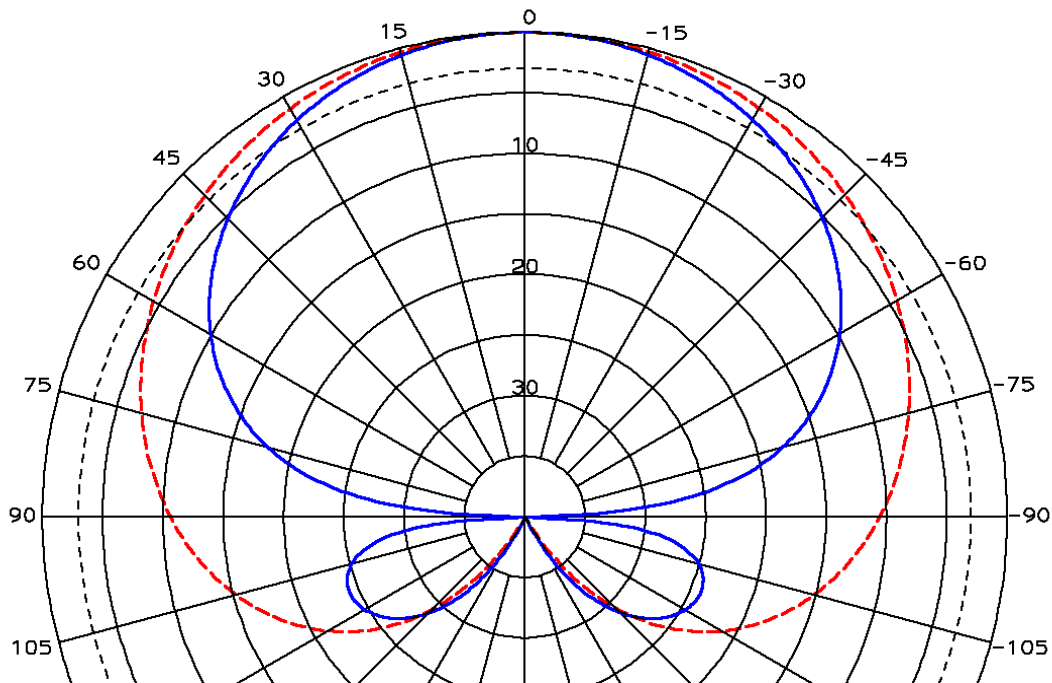
Figure 1-8.1.1-2 Gaussian Beam pattern



### Cardiod Pattern with *E*-plane Null (Dipole)

Many antennas produce patterns with a null at  $\theta = 90^\circ$  because they are constructed using dipoles or resonant loops. This approximation includes this null.

70° *E*-plane Beamwidth, 100° *H*-plane Beamwidth



**Figure 1-8.1.1-3 Cardioid Beam with *E*-plane Null pattern**

Pattern Approximation:

$$E(\theta) = \cos^{N_E}(\theta/2) \cos(\theta) \quad \text{E-plane}$$

$$E(\theta) = \cos^{N_H}(\theta/2) \quad \text{H-plane}$$

*E*-plane exponent given beamwidth and beamwidth level:

$$N_E = \frac{-L_{vl}(dB) - 20 \log[\cos(\text{beamwidth}_{L_{vl}(dB)} / 2)]}{20 \log[\cos(\text{beamwidth}_{L_{vl}(dB)} / 4)]}$$

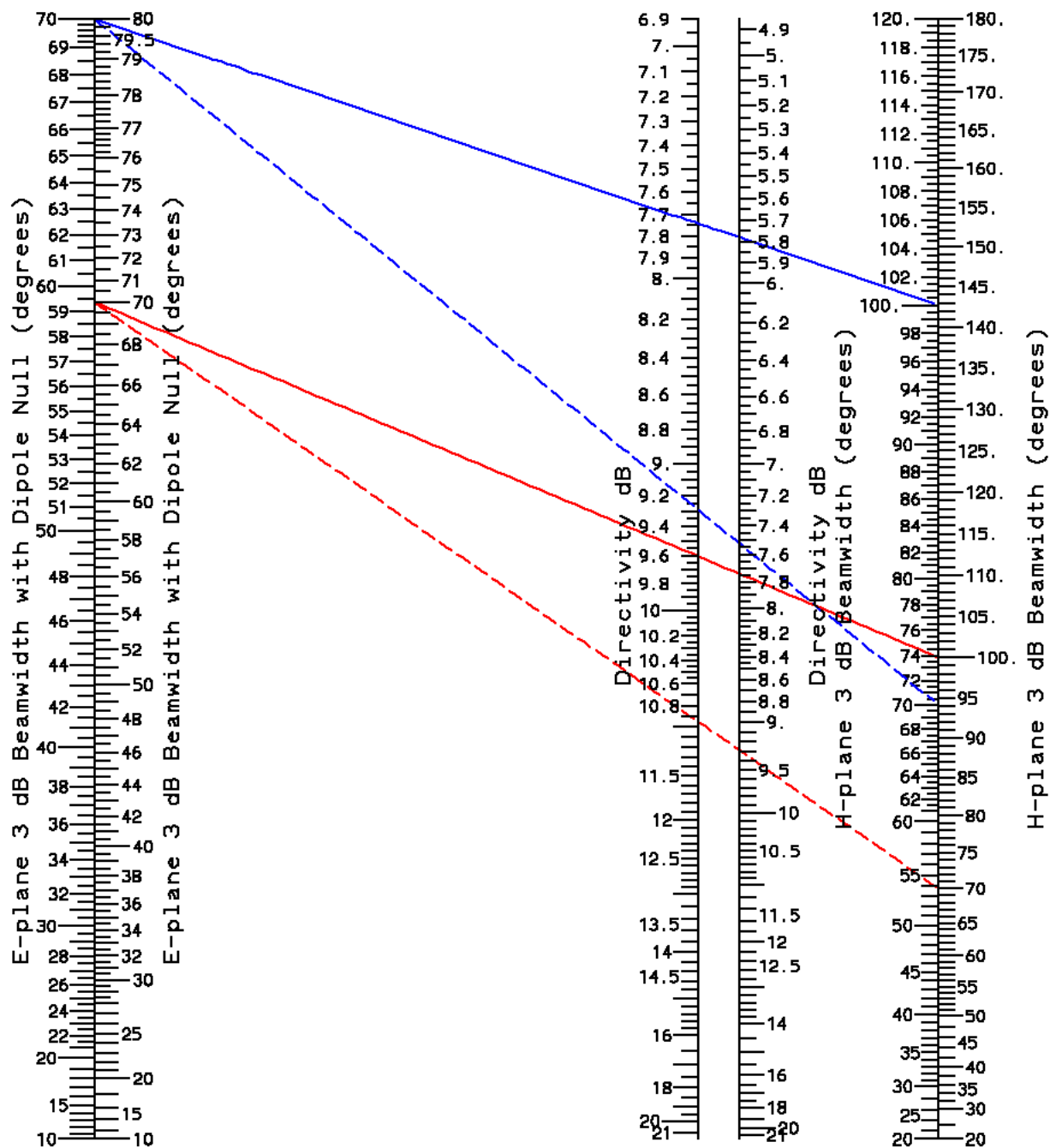
*H*-plane exponent given beamwidth and beamwidth level:

$$N_H = \frac{-L_{vl}(dB)}{20 \log[\cos(\text{beamwidth}_{L_{vl}(dB)} / 4)]}$$

Directivity (Gain) given exponents:

$$Directivity(ratio) = \frac{2}{\frac{1}{N_E + 1} + \frac{4}{N_E + 2} + \frac{4}{N_E + 2} + \frac{1}{N_H + 1}}$$

Use routine **WIDEDDIR** to compute directivity from beamwidths in DOS window



Red example lines use right scales and Blue example lines use left scales

**Figure 1-8.1.1-4 Cardioid Beam with *E*-plane Null pattern Directivity Nomograph**

### $\cos^N(\theta)$ pattern with equal beamwidths in the principal planes

This pattern is often used as a feed for a parabolic reflector. This pattern only radiates above  $\theta = 90^\circ$  with a null in all planes at  $\theta = 90^\circ$ . The pattern has a higher directivity for the same beamwidths than the ones given above. The program **WIDEDIR** computes directivity in a DOS window given  $E$ - and  $H$ -plane beamwidths by using the elliptical approximation of Eq. (1-21).

